|  | Circle | Ellipse | Parabola | Hyperbola |
| :---: | :---: | :---: | :---: | :---: |
| Cone-plane intersection description | Plane's normal is parallel to the cone axis | Plane's normal makes makes a positive angle with cone axis. Angle is less than cone angle. | Plane's normal makes an angle with the cone axis which is equal to cone angle. | Plane's normal makes an angle with cone axis which is greater than the cone angle. |
| Has a focus-locus description | YES | YES | NO | YES |
|  | $\|P F\|=C$ | $\left\|P F_{1}\right\|+\left\|P F_{2}\right\|=C$ | - | $\left\|P F_{1}\right\|-\left\|P F_{2}\right\|=C$ |
| Has a focus-directrix description | NO | YES | YES | YES |
|  | - | $\begin{gathered} \left\|P F_{1}\right\|=\epsilon\|P D\| \\ 0<\epsilon<1 \end{gathered}$ | $\left\|P F_{1}\right\|=\|P D\|$ | $\begin{aligned} \left\|P F_{1}\right\| & =\epsilon\|P D\| \\ \epsilon & >1 \end{aligned}$ |
| Standard cartesian description | $x^{2}+y^{2}=a^{2}$ | $\begin{gathered} (x / a)^{2}+(y / b)^{2}=1 \\ a \geq b>0 \text { or } \\ b \geq a>0 \end{gathered}$ | $\begin{gathered} x^{2}= \pm 4 p y \\ \text { or } \\ y^{2}= \pm 4 p x \end{gathered}$ | $\begin{gathered} (x / a)^{2}-(y / b)^{2}=1 \\ \text { or } \\ (y / b)^{2}-(x / a)^{2}=1 \end{gathered}$ |
| Standard polar description | $\begin{gathered} r=l /(1 \pm \epsilon \cos (\theta)) \\ \text { or } r=l /(1 \pm \epsilon \sin (\theta)) \\ \text { with } \epsilon=0 \end{gathered}$ | with $0<\epsilon<1$ | with $\epsilon=1$ | with $\epsilon>1$ |

## Standard Cartesian Conics.

Note that for the ellipse $x^{2} / a^{2}+y^{2} / b^{2}=1$ (with $a>b$ ) we have foci at ( $\pm c, 0$ ) where $c^{2}=a^{2}-b^{2}$.
For the hyperbola $x^{2} / a^{2}-y^{2} / b^{2}=1$ we have focus at $( \pm c, 0)$ where $c^{2}=a^{2}+b^{2}$. Asymptotes are $y= \pm(b / a) x$. For parabola $x^{2}=4 p y$ we have directrix at $y=-p$ and focus at $(0, p)$.
Other standard equations are obtained by rotating these examples through $\pi / 2, \pi$ and $3 \pi / 2$ radians.

## Standard Polar Conics.

For $\epsilon>0$ the equation $r=l /(1+\epsilon \cos (\theta))$ has one focus at the origin, and directrix at $x=d$.
Here $d$ is found from the equation $\epsilon d=l$.
The 3 other standard polar equations arise by taking $\pi / 2, \pi$ and $3 \pi / 2$ rotations of this conic.

## Polar Coordinates.

Arclength $L=\int_{\alpha}^{\beta} \sqrt{r^{2}+(d r / d \theta)^{2}} d \theta$.
Area $A=(1 / 2) \int_{\alpha}^{\beta} r^{2} d \theta$.
Parametric Curves.
Arclength $L=\int_{a}^{b} \sqrt{(d x / d t)^{2}+(d y / d t)^{2}} d t$.

